

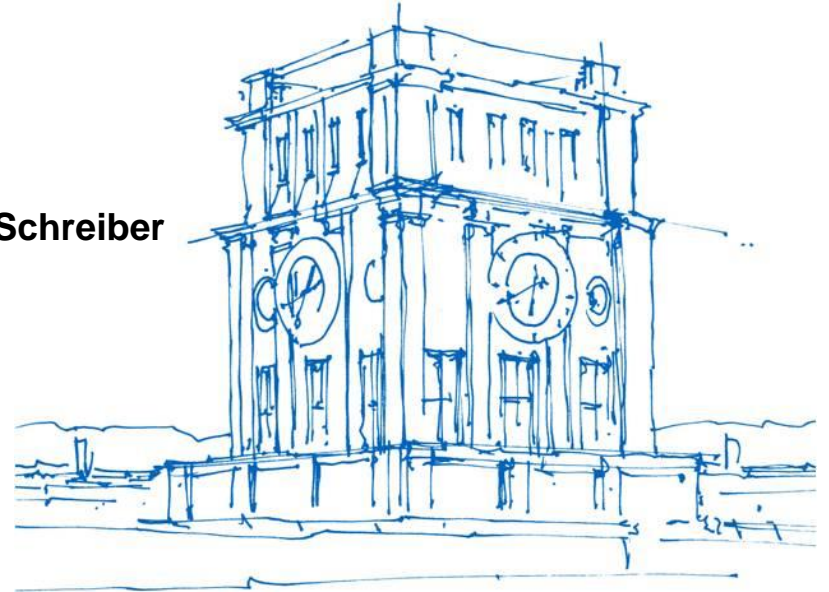
ELT Data Processing – about Noise, Calibration Capability and Synergies

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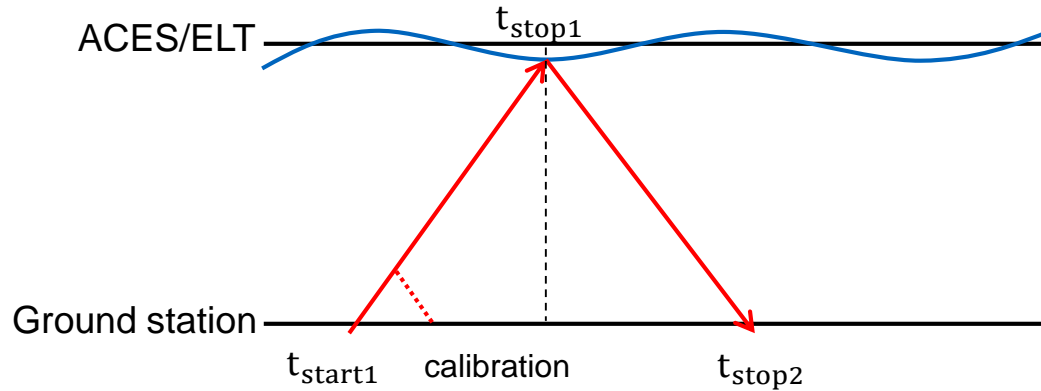
Uhrenturm der TUM

ELT Data Processing – about Noise, Calibration Capability and Synergies

1. **European Laser Timing:** Measurement principle and data analysis
2. **Complications I:** due to ISS
3. **Complications II:** Complexity of the measurement on ground
4. **Comparison:** ELT versus MWL
5. **Synergies:** ELT and microwave techniques

Measurement principle

Optical link, pulsed



Measurement principle

Principle of ELT (optical link, pulsed)

- One way:

$$tof_{1W} = R_{CoM} + \tau_{troposphere} + \tau_{Sagnac} + \tau_{Shapiro} + \tau_{attitudeDetector}$$

- Round trip:

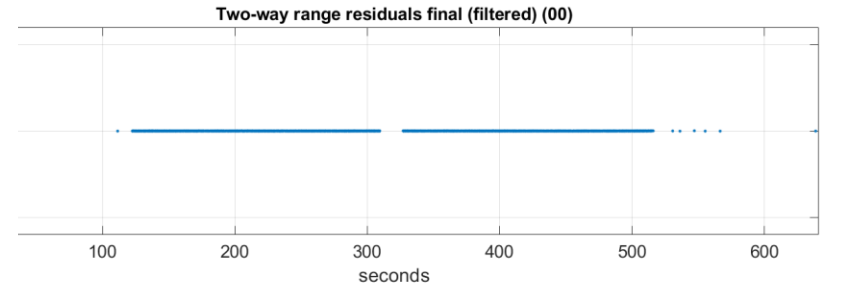
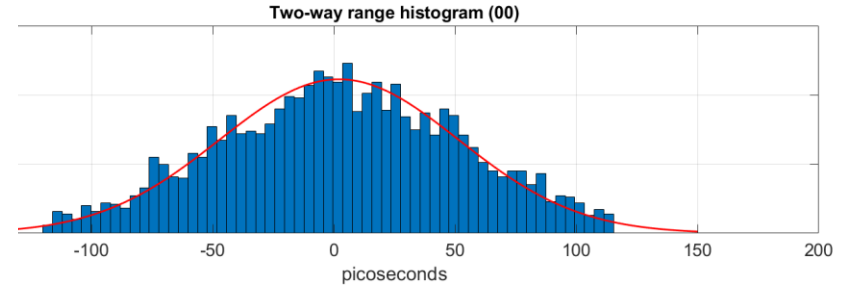
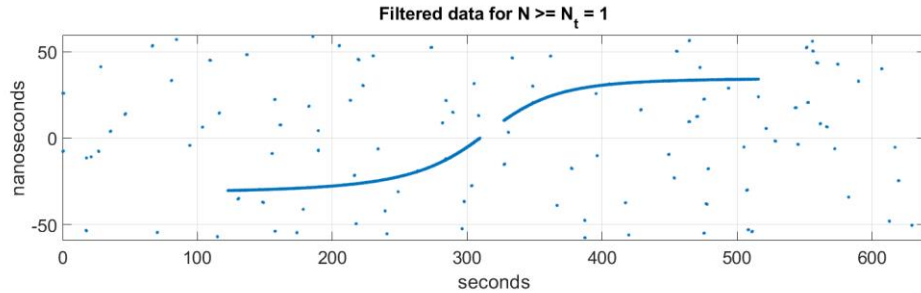
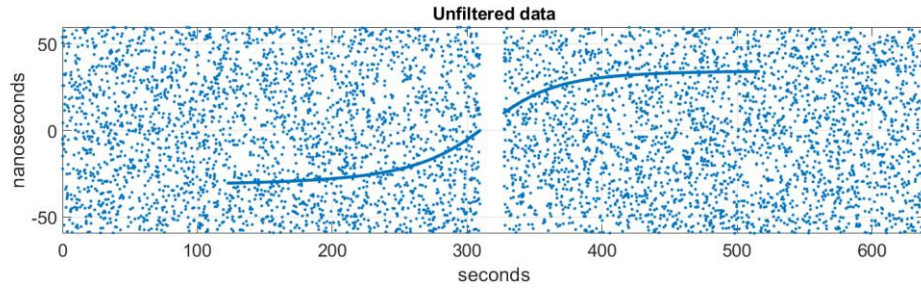
$$tof_{2W} = 2 * (R_{CoM} + \tau_{troposphere} + \tau_{Shapiro} + \tau_{attitudeReflector}) + \tau_{Reflector}$$

with R_{CoM} : Distance between spacecraft CoM and station reference point

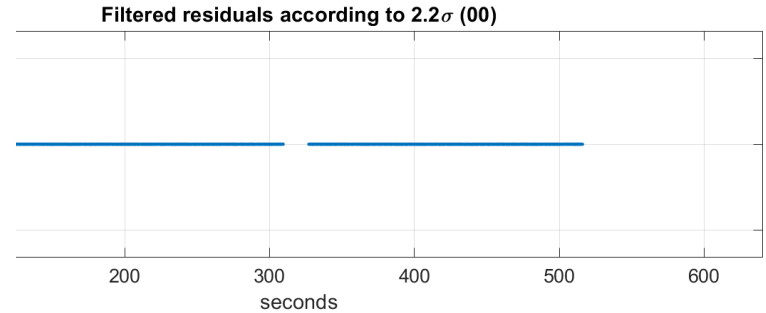
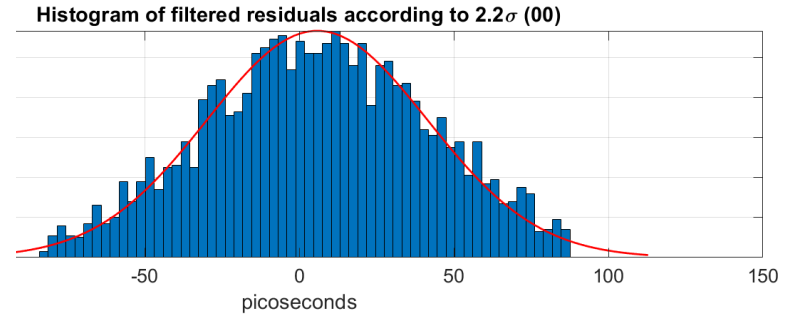
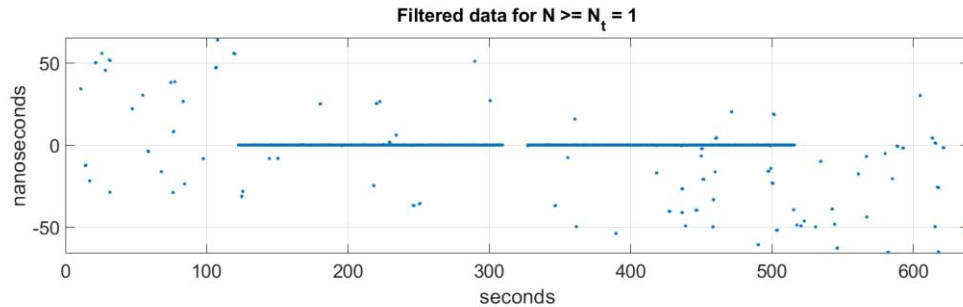
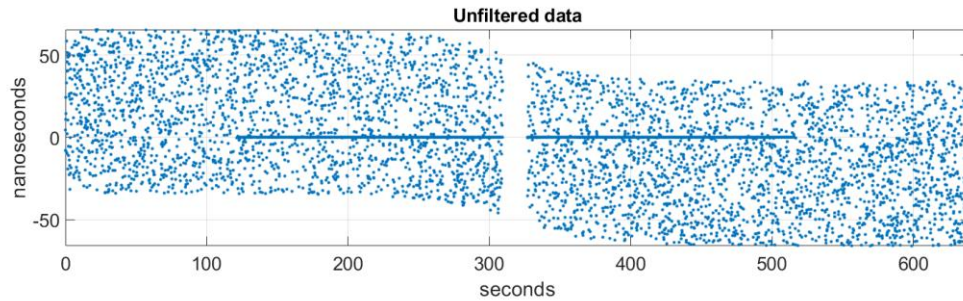
- Time transfer:

$$\tau = \frac{t_{return} + t_{start}}{2} - t_{detector} + \tau_{corr} = \frac{tof_{2W}}{2} + t_{start} - t_{detector} + \tau_{corr}$$

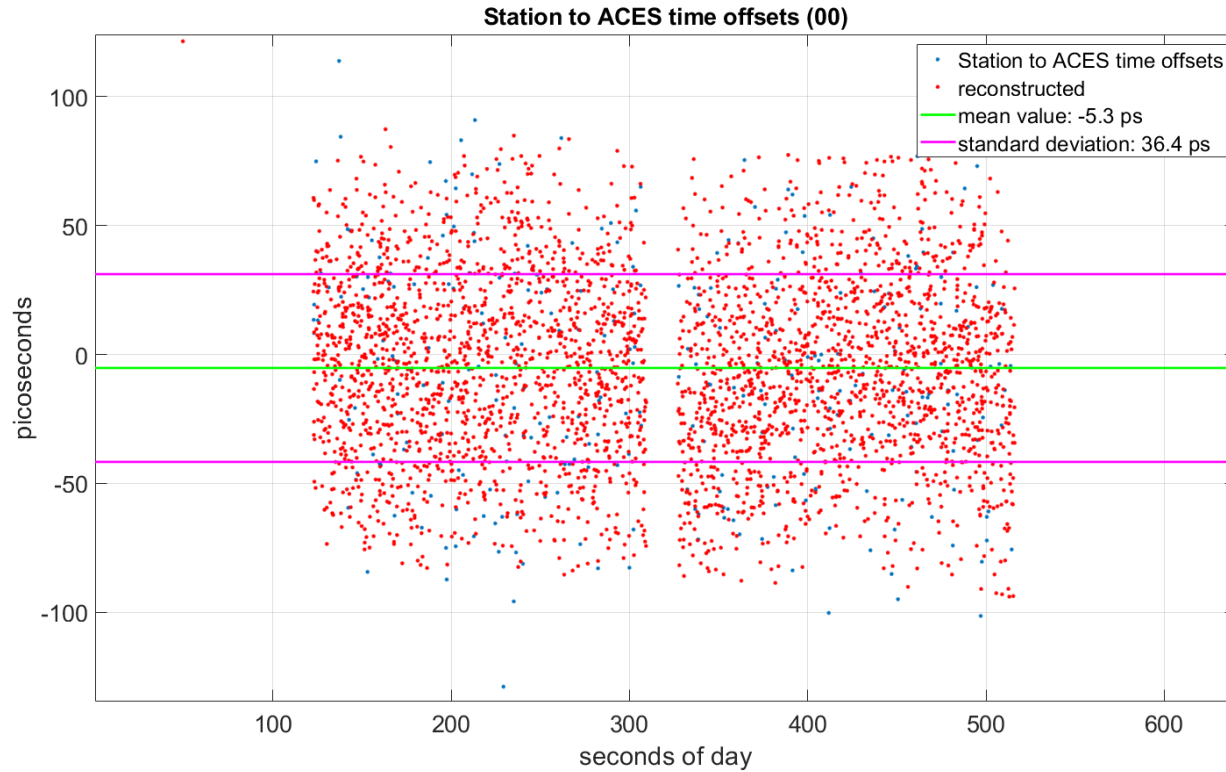
Round-trip measurements



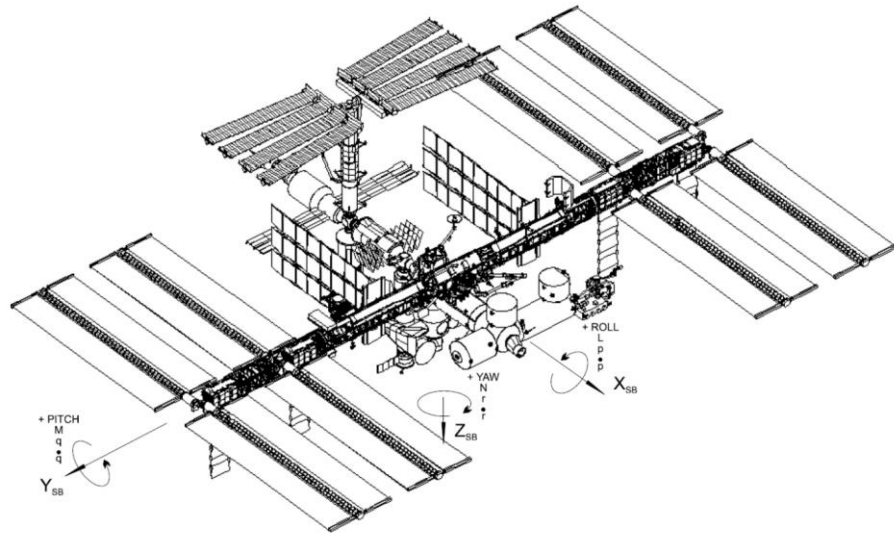
One-way measurements



Time transfer



Multireflector problem



<i>Name</i>	<i>X [m]</i>	<i>Y [m]</i>	<i>Z [m]</i>
<i>JEM LRR Hemi A</i>	10.878	-5.448	7.021
<i>JEM LRR Hemi B</i>	10.876	-6.092	7.017
<i>IDA 1 Hemi B (a)</i>	15.789	0.891	6.239
<i>C2V2 S3 Forward Antenna Boom Hemi (c)</i>	1.524	22.887	-1.417
<i>C2V2 P3 Nadir Antenna Boom Hemi (c)</i>	-2.621	-22.887	-0.978

Multireflector problem

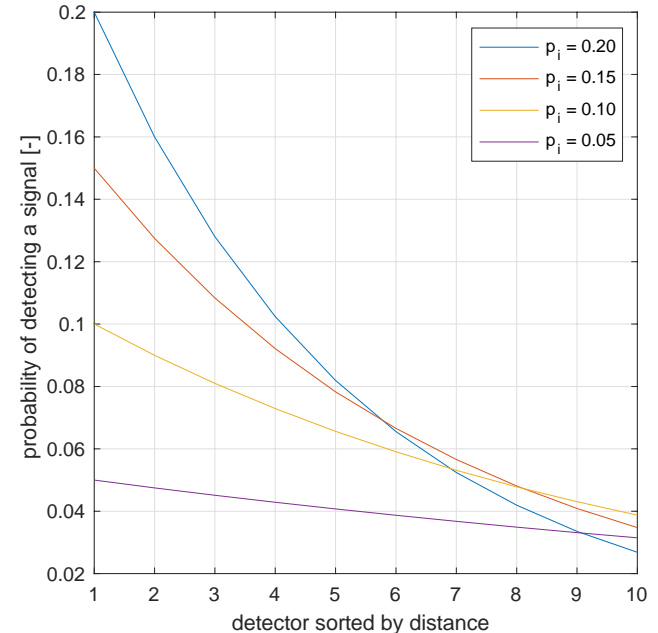
For reflectors $i = 0 \dots N$ with distances $d_i \leq d_{i+1}$ with respect to the observer the probability of detecting a signal is:

$$p_{i,eff} = p_i \prod_{j=0}^{i-1} (1 - p_j)$$

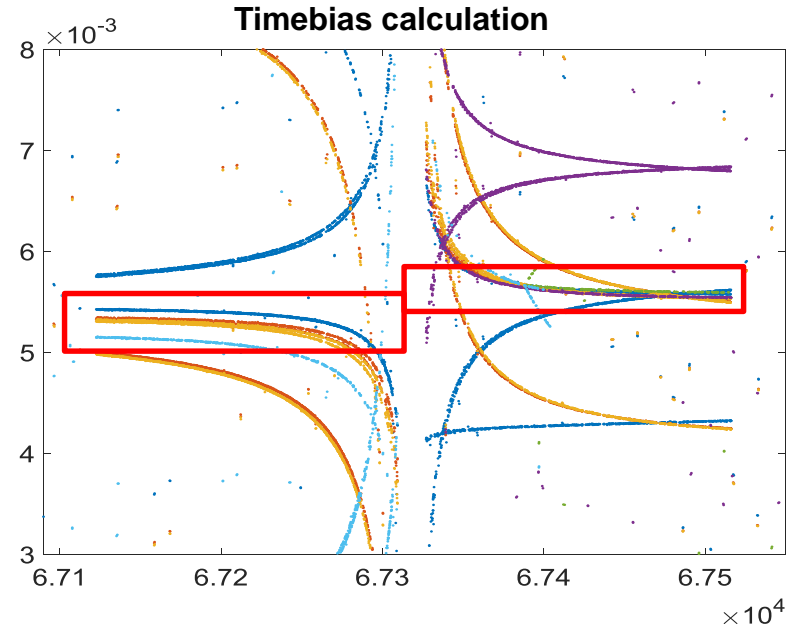
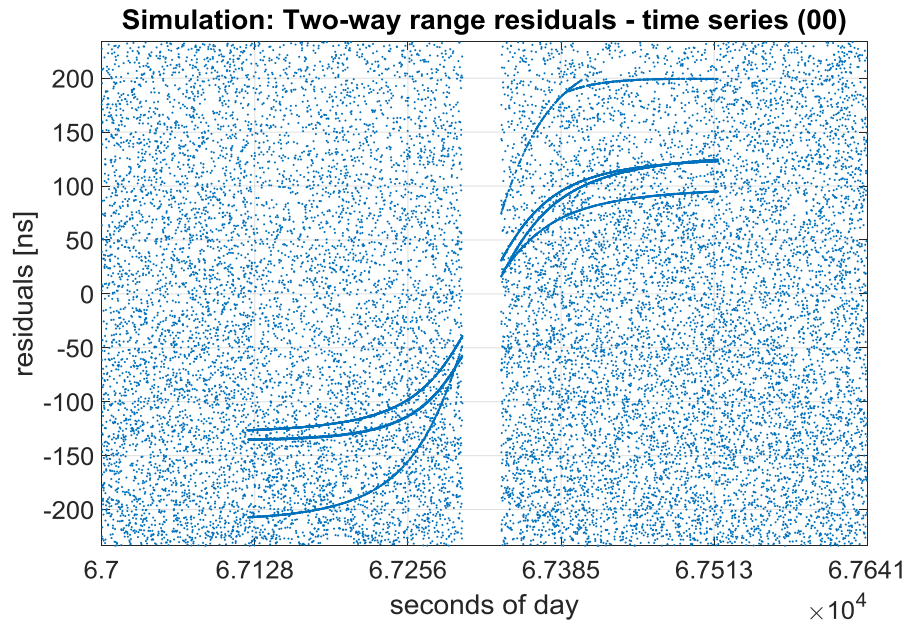
The single-reflector probabilities p_i may account for differences in the effective cross section among the reflectors.

With a constant background noise rate, the noise statistics follows an exponential distribution in single photon mode:

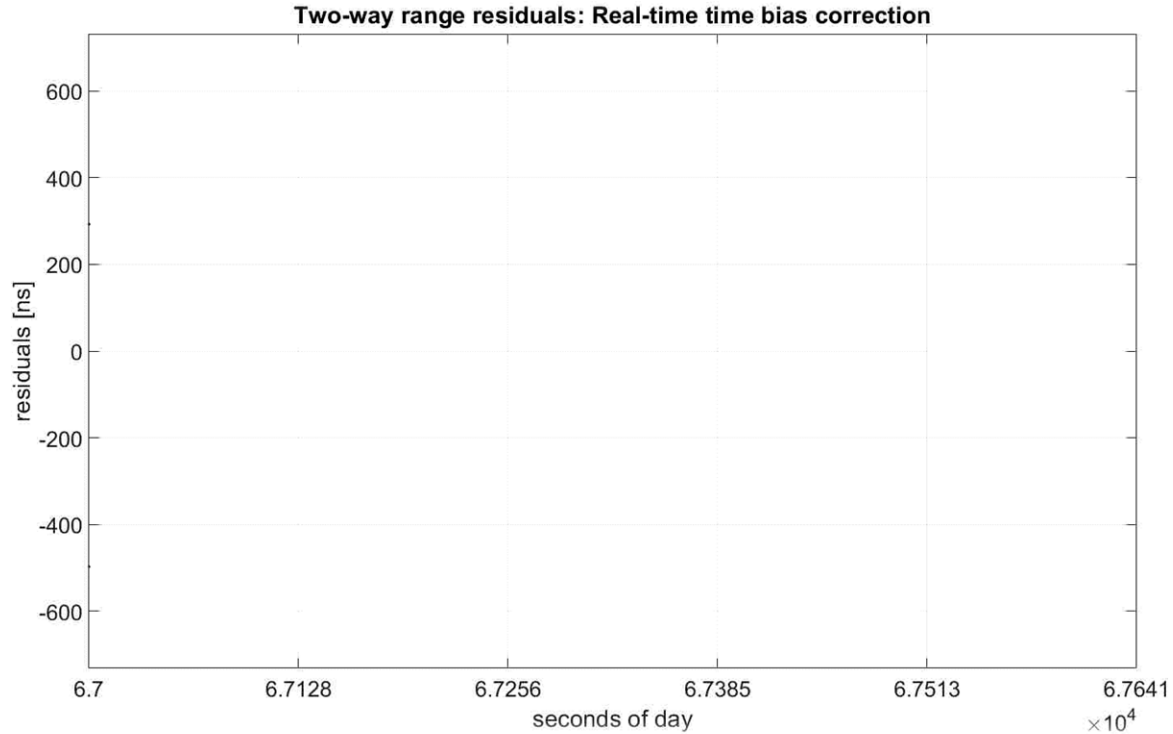
$$p_{signal,i} = p_{eff,i} e^{-n_{noise} \Delta t_i}$$



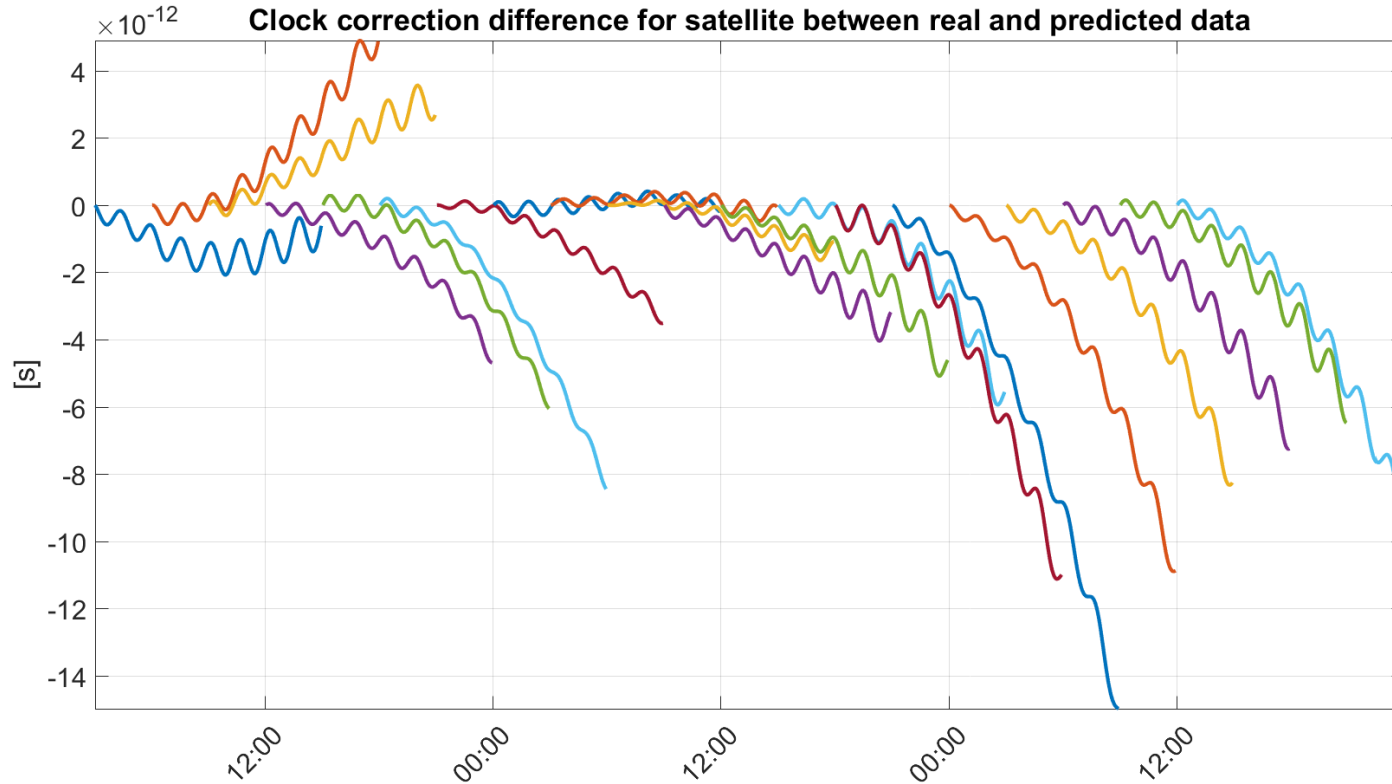
Detector identification



Complexity of ELT for ground stations



ACES clock prediction



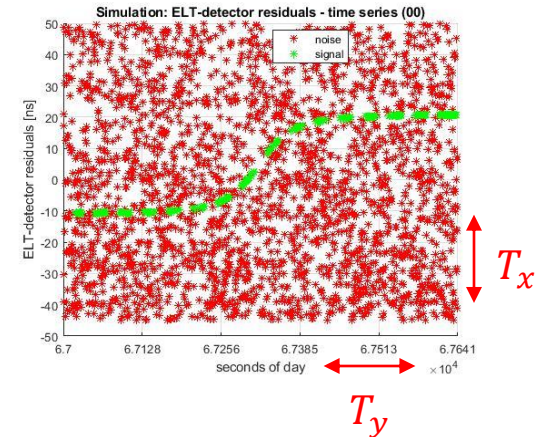
New noise reduction algorithm

$$P_{s>thr} = \sum_{m=N_t}^{\infty} p_{binomial,n+s}(m) \quad P_{n+s}(T_x) = 1 - \exp[-(n_n T_x + N_s)]$$

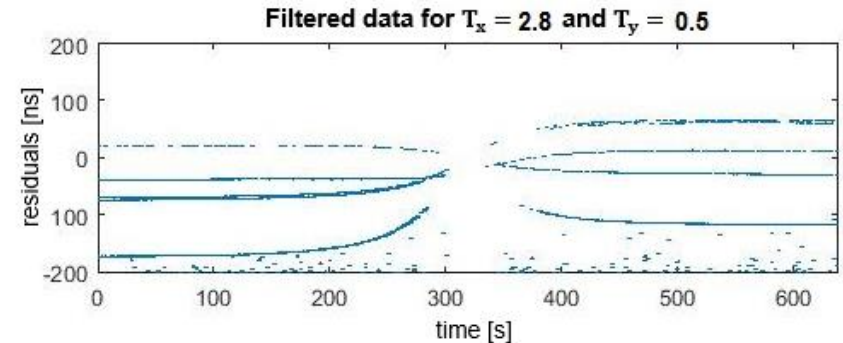
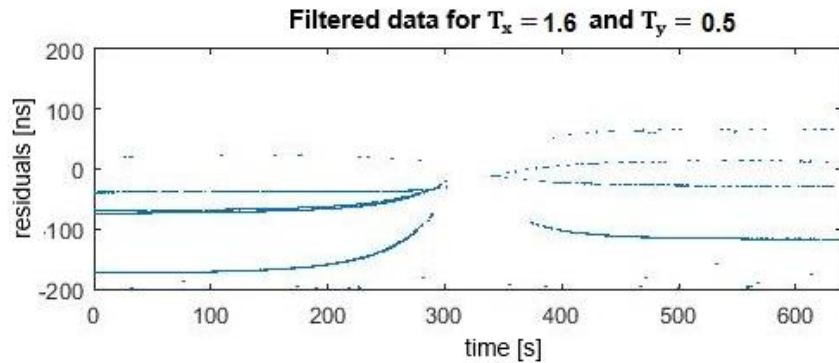
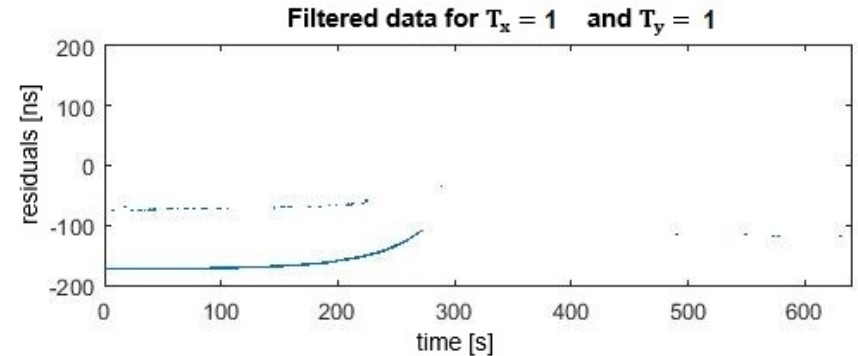
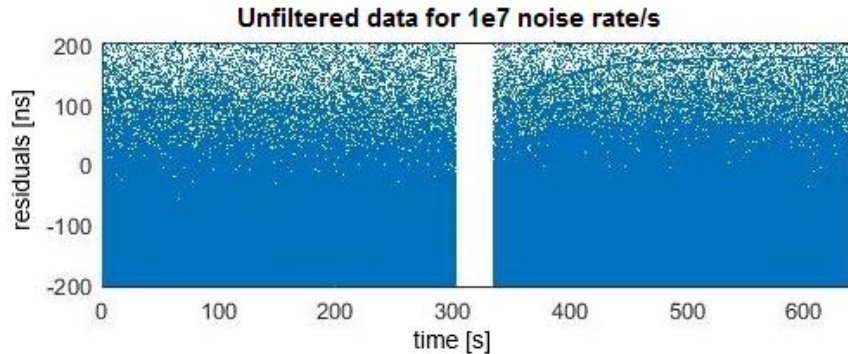
$$p_{binomial,n+s}(m) = \frac{y!}{m!(y-m)!} P_{n+s}(T_x)^m (1 - P_{n+s}(T_x))^{y-m}$$

$$P_{n>thr} = \sum_{m=N_t}^{\infty} p_{binomial,n}(m) \quad P_n(T_x) = 1 - \exp[-n_n T_x]$$

$$p_{binomial,n}(m) = \frac{y!}{m!(y-m)!} P_n(T_x)^m (1 - P_n(T_x))^{y-m}$$



New noise reduction algorithm



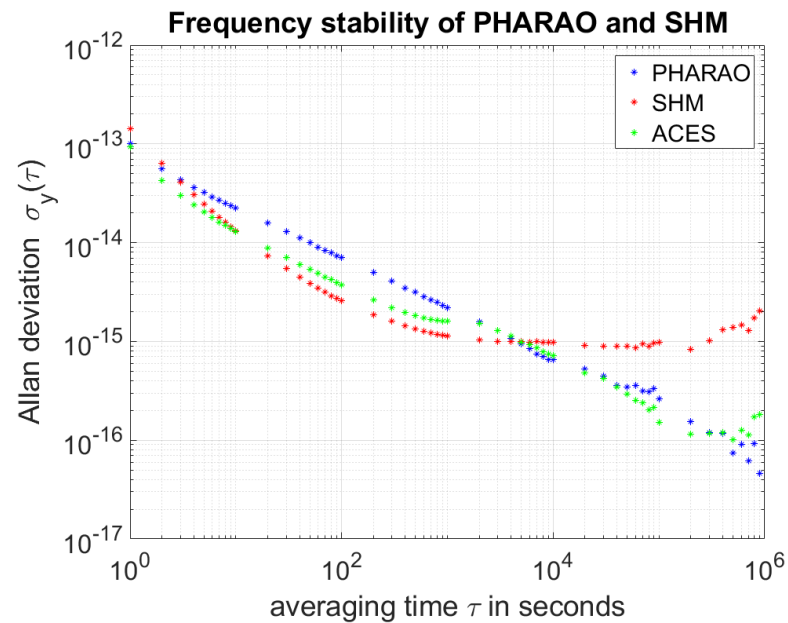
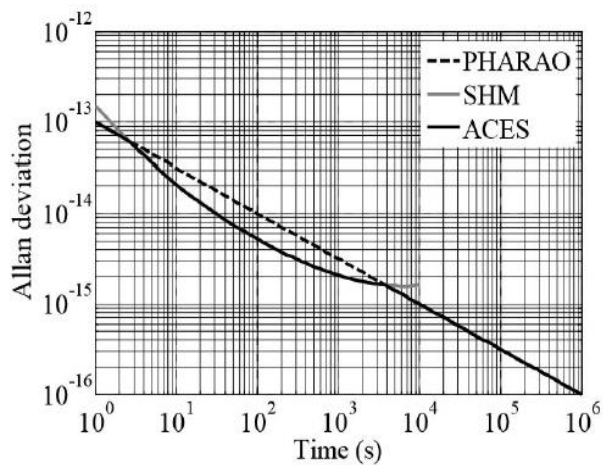
Geometric components

- ISS attitude simulation
(3 axes, constant offsets and oscillations)
- Detector and multi reflector positions
- Intra-reflector delay (function of incidence angle)
- Visibility constraints (minimum elevation, clouds)
- Tidal motion and atmospheric loading

Stochastic components

- Background noise
- Laser Jitter
- Pulse width
- Clock noise and offsets
- (Fluctuations in the troposphere)

Clock simulation



Ground segment



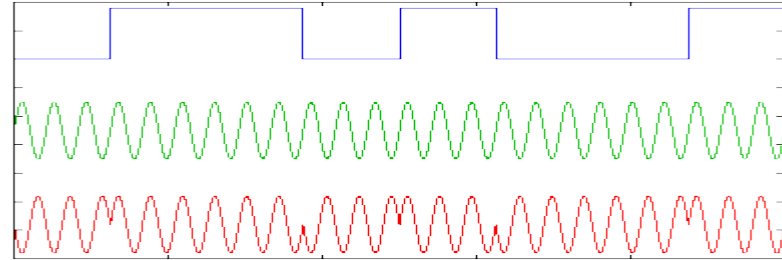
Comparison with MWL

ELT:



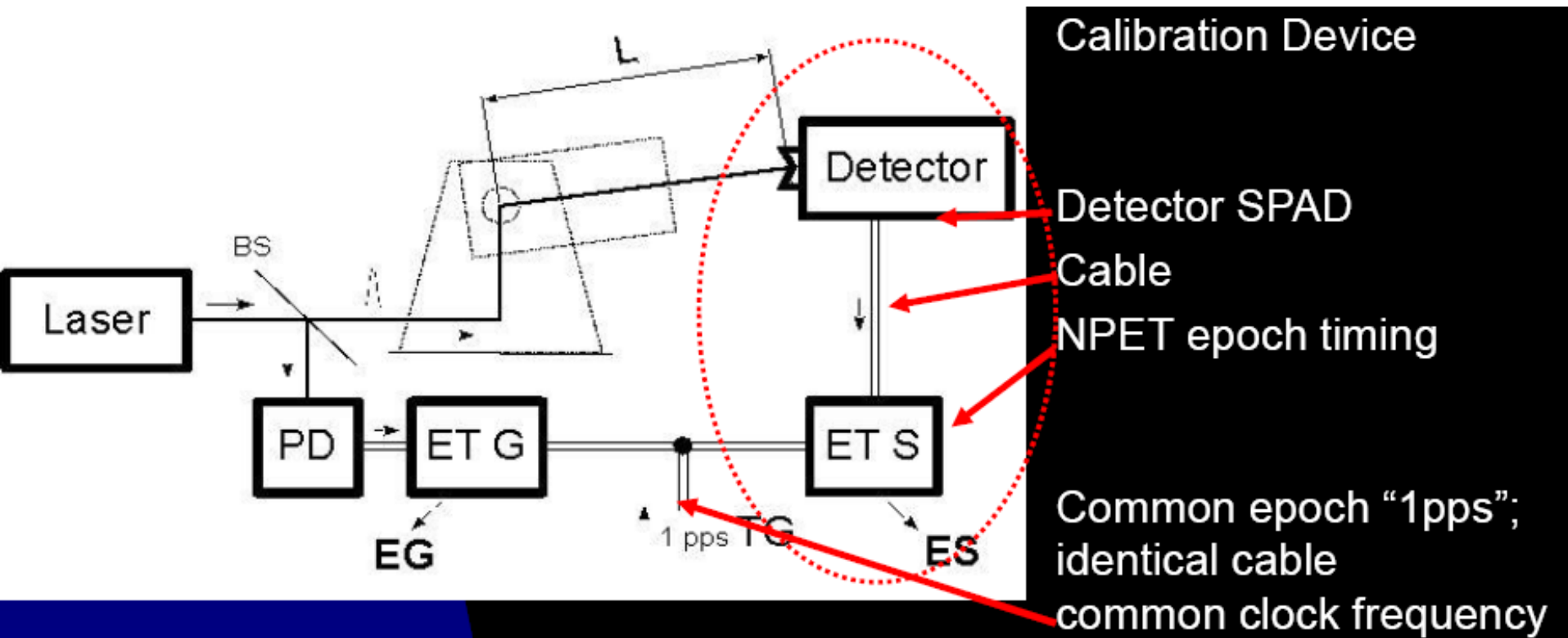
Optical -> calibration -> 50 ps accuracy
no wet tropospheric delay
Time tagging of events -> jitter per detection
pulse length 10 ps / 1 kHz -> 4 ps @ 300s
7ps @ 1 d

MWL:

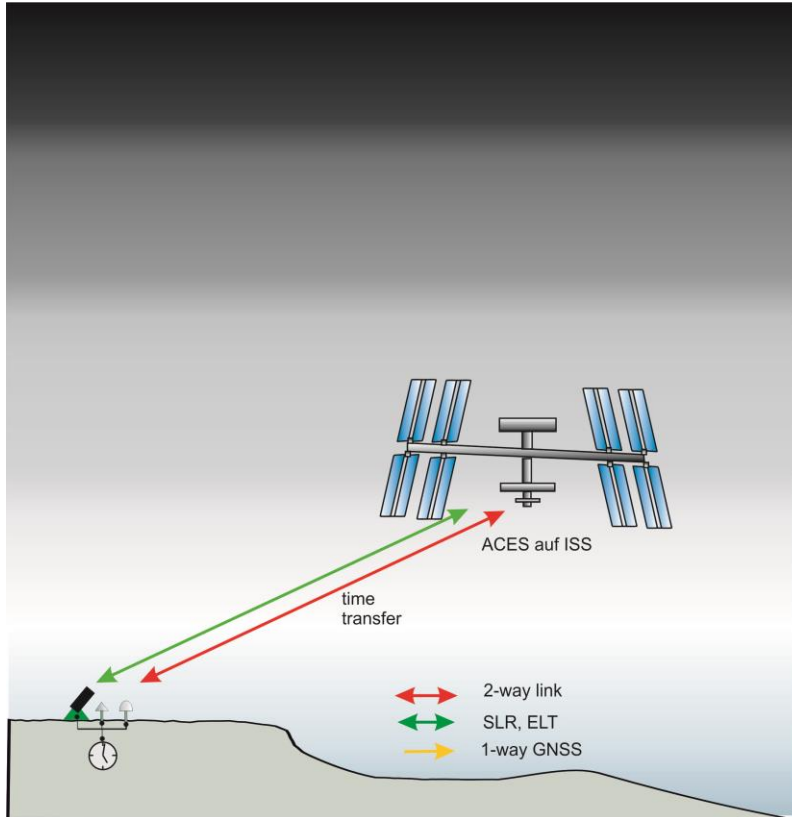


Microwave -> no calibration -> 100 ps accuracy
wet tropospheric delay
Phase locked loop -> jitter per contact
100 Mchip/s / 14 GHz -> 230 fs @ 300s
8 ps @ 1 d

Calibration

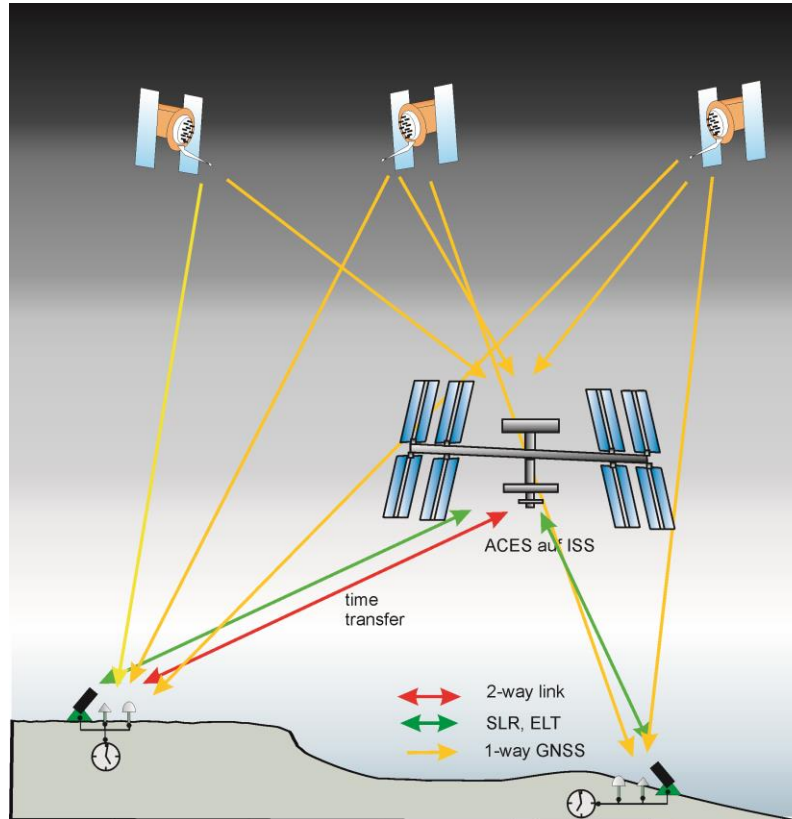


Calibration of MWL



- ⇒ Calibration of MWL for time transfer and ranging
- ⇒ Troposphere
- ⇒ Short arc orbit adjustment
- ⇒ Systematic effects
- ⇒ Try a common parameter estimation and compare to time transfer in Lambda configuration

Calibration of GNSS links



- ⇒ Calibration of GNSS receiver
- ⇒ T2L2 only in common-view
- ⇒ ELT now also in non-common-view

Conclusions



ELT Data Center delivers the following products:

Space to ground clock comparison

Ground to ground clock comparison in common-view

Ground to ground clock comparison in non-common-view

MWL calibration